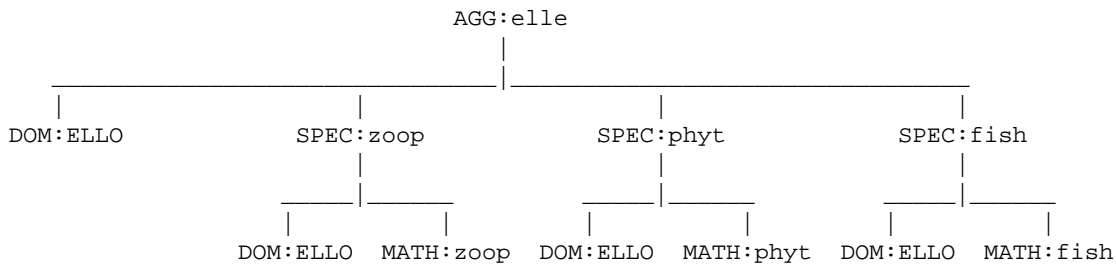


# ellebo lake (Version: 0)

ECOBAS Documentation (ECOBAS\_MIF 3.1) \*

9th August 2004

## 1 Structure



## 2 AGG: ellebo lake (Version: 0)

**Domain identifier:** ELLOBO (see section: 9)

**Author:** Angelini,Ronaldo

**Documented by:** Benz,Joachim

**Model (Origin of this mathematical formulation):**

ELLOBO; A model for the plankton system of the Broa reservoir, Sao Carlos, Brazil

**References:** [Ang00]

**Keywords:** undefined

### 2.1 Structure of the aggregate

#### 2.1.1 Declaration of variables

| acronym            | description            |
|--------------------|------------------------|
| INPUT:             |                        |
| <i>temperature</i> | temperature (of water) |

#### 2.1.2 Components

| Name of module             | Type of module |
|----------------------------|----------------|
| zooplankton (version: 0)   | DYNAMIC        |
| phytoplankton (version: 0) | DYNAMIC        |
| fish (version: 0)          | DYNAMIC        |

\*Database: /eco6/benz/\_ecobas/db/dbb/

### 2.1.3 Connections

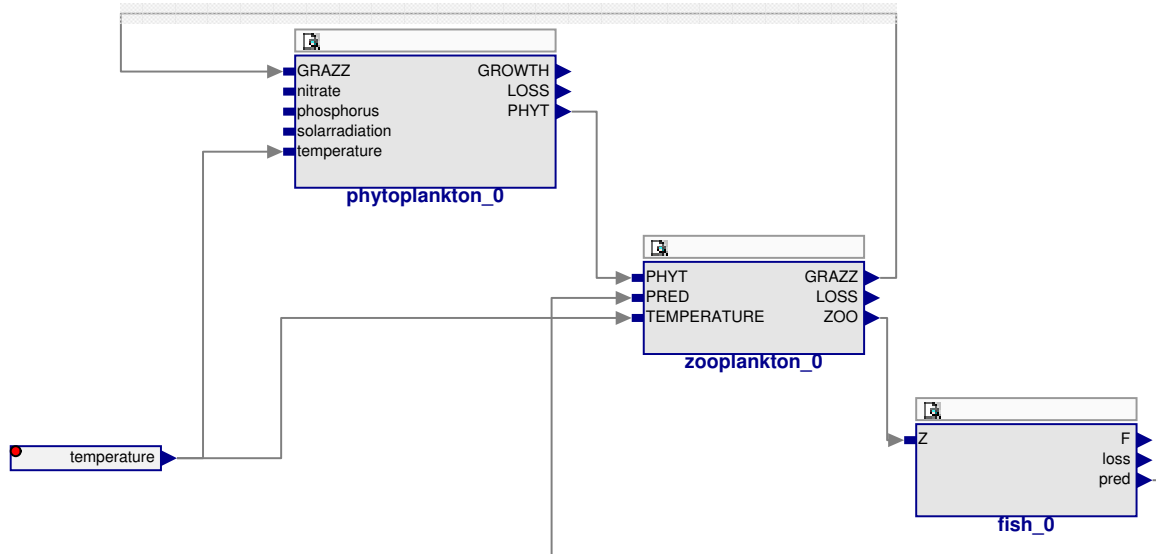
| <i>source module:variable</i> | ↦ | <i>sink module:variable</i>        |
|-------------------------------|---|------------------------------------|
| <i>phytoplankton_0:PHYT</i>   | ↦ | <i>zooplankton_0:PHYT</i>          |
| <i>zooplankton_0:GRAZZ</i>    | ↦ | <i>phytoplankton_0:GRAZZ</i>       |
| <i>zooplankton_0:ZOO</i>      | ↦ | <i>fish_0:Z</i>                    |
| <i>fish_0:pred</i>            | ↦ | <i>zooplankton_0:PRED</i>          |
| <i>INPUT:temperature</i>      | ↦ | <i>phytoplankton_0:temperature</i> |
| <i>INPUT:temperature</i>      | ↦ | <i>zooplankton_0:TEMPERATURE</i>   |

## 2.2 Description of Specification

Template Content

## 2.3 List of figures

Figure(1): ellebo\_lake\_0.s.eps



## 3 SPEC: zooplankton (Version: 0)

**Instance of MATH module:** zooplankton (Version: 1)

**Domain identifier:** ELLOBO (see section: 9)

**Author:** Petrerre,Miguel

**Author:** Angelini,Ronaldo

**Documented by:** Noeding,Dirk

**Model (Origin of this mathematical formulation):**

ELLOBO; A model for the plankton system of the Broa reservoir, Sao Carlos, Brazil

**References:** [Ang00]

**Keywords:** biomass

### 3.1 Declaration of Quantities

| acronym     | unit    | meaning       | method | value | range   | indomain |
|-------------|---------|---------------|--------|-------|---------|----------|
| $t$         | $d$     |               |        |       | 0 : 365 |          |
| $ZOO_0$     | $mug/l$ | concentration |        | 0.1   |         |          |
| $k_{phyt}$  | $l/mug$ | —             |        | 1.0   |         |          |
| $ZOO_{up}$  | $mug/l$ | —             |        | 3.3   |         |          |
| $ZOO_{low}$ | $mug/l$ | —             |        | 0.8   |         |          |
| $M_{zoo}$   | $1/d$   | —             |        | 0.3   |         |          |

continued on next page

| <i>continued from previous page</i> |                 |                |        |       |       |          |
|-------------------------------------|-----------------|----------------|--------|-------|-------|----------|
| acronym                             | unit            | meaning        | method | value | range | indomain |
| $TEMPERATURE_{max}$                 | $C$             | –              |        | 27.1  |       |          |
| $C_k$                               | $mug/l$         | –              |        | 3.3   |       |          |
| $K_z$                               | $1/d$           | –              |        | 0.5   |       |          |
| $PRED$                              | $mug/(l * d)$   | –              |        |       |       |          |
| $TEMPERATURE$                       | $C$             | –              |        | 23    |       |          |
| $PHYT$                              | $mug/l$         | <i>biomass</i> |        | 4.0   |       |          |
| $ZOO$                               | $mug/l$         | <i>biomass</i> |        |       |       |          |
| $PHYT_{av}$                         | <i>unitless</i> | –              |        |       |       |          |
| $GRAZZ$                             | $mug/(l * d)$   | –              |        |       |       |          |
| $M_{yz}$                            | $1/d$           | –              |        |       |       |          |
| $LOSS$                              | $mug/(l * d)$   | –              |        |       |       |          |

## 4 SPEC: phytoplankton (Version: 0)

**Instance of MATH module:** phytoplankton (Version: 0)

**Domain identifier:** ELLOBO (see section: 9)

**Author:** Angelini,Ronaldo

**Documented by:** Noeding,Dirk

**Model (Origin of this mathematical formulation):**

ELLOBO; A model for the plankton system of the Broa reservoir, Sao Carlos, Brazil

**References:** [Ang00]

**Keywords:** nitrogen, Phytoplankton, grazing, light, phosphor

### 4.1 Declaration of Quantities

| acronym               | unit            | meaning              | method | <i>value</i> | <i>range</i> | indomain |
|-----------------------|-----------------|----------------------|--------|--------------|--------------|----------|
| $t$                   | $d$             |                      |        |              |              |          |
| $PHYT_0$              | $mug/l$         | <i>concentration</i> |        | 1.0          |              |          |
| $K_c$                 | $1/d$           | –                    |        | 0.2          |              |          |
| $K_{sr}$              | $mumol$         | –                    |        | 140          |              |          |
| $K_{pd}$              | $mug/l$         | –                    |        | 1.1          |              |          |
| $K_{nt}$              | $mug/l$         | –                    |        | 0.5          |              |          |
| $G_{phyt}$            | $mug/l/d$       | –                    |        | 0.5          |              |          |
| $GRAZZ$               | $mug/l/d$       | –                    |        | 0.0          |              |          |
| <i>solarradiation</i> | $mumol$         | –                    |        |              |              |          |
| <i>nitrate</i>        | $mug/l$         | –                    |        |              |              |          |
| <i>phosphorus</i>     | $mug/l$         | –                    |        |              |              |          |
| <i>temperature</i>    | $C$             | –                    |        | 23           |              |          |
| $PHYT$                | $mug/l$         | –                    |        |              |              |          |
| $GROWTH$              | $mug/l/d$       | –                    |        |              |              |          |
| $LOSS$                | $mug/l/d$       | –                    |        |              |              |          |
| $G_{max}$             | $mug/l/d$       | –                    |        |              |              |          |
| $MM_{sr}$             | <i>unitless</i> | –                    |        |              |              |          |
| $MM_{nt}$             | <i>unitless</i> | –                    |        |              |              |          |
| $MM_{pd}$             | <i>unitless</i> | –                    |        |              |              |          |

## 5 SPEC: fish (Version: 0)

**Instance of MATH module:** fish (Version: 1)

**Domain identifier:** ELLOBO (see section: 9)

**Documented by:** Noeding,Dirk

**Model (Origin of this mathematical formulation):**

ELLOBO; A model for the plankton system of the Broa reservoir, Sao Carlos, Brazil

**References:** [Ang00]

**Keywords:** biomass, Astyanax fasciatus, predation

## 5.1 Declaration of Quantities

| acronym | unit          | meaning | method | value | range | indomain |
|---------|---------------|---------|--------|-------|-------|----------|
| $t$     | $d$           |         |        |       |       |          |
| $K_l$   | $1/d$         | –       |        | 0.5   |       |          |
| $K_p$   | $1/d$         | –       |        | 0.24  |       |          |
| $Z$     | $mug/l$       | –       |        |       |       |          |
| $F$     | $mug/l$       | –       |        |       |       |          |
| $pred$  | $mug/(l * d)$ | –       |        |       |       |          |
| $loss$  | $mug/(l * d)$ | –       |        |       |       |          |

## 6 MATH: zooplankton (Version: 1)

**Author:** Petreire,Miguel

**Author:** Angelini,Ronaldo

**Documented by:** Noeding,Dirk

**Model (Origin of this mathematical formulation):**

ELLOBO; A model for the plankton system of the Broa reservoir, Sao Carlos, Brazil

**References:** [Ang00] [Joe83]

**Keywords:** biomass, population dynamics, zooplankton

**Simtype:** DYNAMIC

### 6.1 Declaration of Variables

| acronym       | type* | description                                     | time scale | time agg. | intime/state type |
|---------------|-------|---|------------|-----------|-------------------|
| DEPENDENT:    |       |   |            |           |                   |
| $PHYT_{av}$   | FM    | availability of phytoplankton for grazing       |            | none      |                   |
| $GRAZZ$       | FM    | predation of zooplankton on phytoplankton       |            | none      |                   |
| $M_{yz}$      | FM    | temperatur dependent growth rate of zooplankton |            | none      |                   |
| $LOSS$        | FM    | respiration and mortality of zooplankton        |            | none      |                   |
| STATE:        |       |   |            |           |                   |
| $ZOO$         | FM    | biomass of zooplankton                          |            | none      | CONTINUOUS        |
| INPUT:        |       |   |            |           |                   |
| $PRED$        | FM    | feeding by fish                                 |            | none      |                   |
| $TEMPERATURE$ | FM    | temperature of water                            |            | none      |                   |
| $PHYT$        | FM    | biomass of phytoplankton                        |            | none      |                   |
| CONSTANT:     |       |   |            |           |                   |
| $ZOO_0$       | FM    | inital value of zooplankton biomass             |            | none      |                   |
| $k_{phyt}$    | FM    | constant used for phytoplankton availability    |            | none      |                   |
| $ZOO_{up}$    | FM    | upper limit of random number RANZOO             |            | none      |                   |
| $ZOO_{low}$   | FM    | lower limit of random number RANZOO             |            | none      |                   |
| $M_{zoo}$     | FM    | is the calibrated value for growth rate         |            | none      |                   |

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| acronym             | type* | description                            |      |
|---------------------|-------|--|------|
| $TEMPERATURE_{max}$ | FM    | maximale temperature at Broa reservoir | none |
| $C_k$               | FM    | carring capacity for zooplankton       | none |
| $K_z$               | FM    | respiration and mortality per day      | none |
| TIME:               |       |  |      |
| $t$                 |       | time                                   |      |

\*) 1.character: alphanumeric(A) or float(F) or integer(I)

2.character: metric(M) or ordinal(O) or nominal(N)

## 6.2 Equation(s)

### 6.2.1 Initial state of the system ( $t \doteq 0$ ) :

$$\text{Bound: } ZOO = ZOO_0 \quad (1)$$

### 6.2.2 dynamics of zooplankton biomass Equationblock(1)

$$\frac{dZOO}{dt} = GRAZZ - LOSS - PRED \quad (2)$$

$$LOSS = ZOO \cdot K_z \quad (3)$$

### 6.2.3 grazing Equationblock(2)

$$GRAZZ = M_{yz} \cdot PHYT_{av} \cdot \left(1 - \frac{ZOO}{C_k}\right) \cdot RUNIFORM(ZOO_{low}, ZOO_{up}) \quad (4)$$

$$M_{yz} = M_{zoo} \cdot 0.98^{TEMPERATURE - TEMPERATURE_{max}} \quad (5)$$

$$PHYT_{av} = k_{phyt} \cdot PHYT \quad (6)$$

## 6.3 Description of MATH module

Zooplankton in Broa reservoir is represented by Cladocera (13.8%), Copepod (81%) and Rotifers (5.4%). The dynamics of zooplankton is determined by 3 terms:

- grazing of phytoplankton (GRAZZ)
- respiration and mortality (LOSS) and
- feeding of zooplankton by fish (PRED)

Grazing is formulated according ODUM 1972(see: [Joe83], page83). The dependence of amount of zooplankton is formulated here by introducing a uniform distributed random variable.

## 7 MATH: phytoplankton (Version: 0)

**Author:** Angelini,Ronaldo

**Author:** Petreire,Miguel

**Documented by:** Noeding,Dirk

**Model (Origin of this mathematical formulation):**

ELLOBO; A model for the plankton system of the Broa reservoir, Sao Carlos, Brazil

**Keywords:** Phytoplankton, biomass dynamic

**Simtype:** DYNAMIC

## 7.1 Declaration of Variables

| acronym                 | type* | description                                   | time scale | time agg. | intime/state type |
|-------------------------|-------|---|------------|-----------|-------------------|
| DEPENDENT:              |       |   |            |           |                   |
| <i>GROWTH</i>           | FM    | growth rate of phytoplankton                  |            | none      |                   |
| <i>LOSS</i>             | FM    | respiration and mortality of phytoplankton    |            | none      |                   |
| <i>G<sub>max</sub></i>  | FM    | Rate coefficient of temperature               |            | none      |                   |
| <i>MM<sub>sr</sub></i>  | FM    | light   |            | none      |                   |
| <i>MM<sub>nt</sub></i>  | FM    | nitrogen                                      |            | none      |                   |
| <i>MM<sub>pd</sub></i>  | FM    | phosphor                                      |            | none      |                   |
| STATE:                  |       |   |            |           |                   |
| <i>PHYT</i>             | FM    | Phytoplankton                                 |            | none      | CONTINUOUS        |
| INPUT:                  |       |   |            |           |                   |
| <i>GRAZZ</i>            | FM    | predation of zooplankton on phytoplankton     |            | none      |                   |
| <i>solarradiation</i>   | FM    | light   |            | none      |                   |
| <i>nitrate</i>          | FM    | nitrogen                                      |            | none      |                   |
| <i>phosphorus</i>       | FM    | phosphor                                      |            | none      |                   |
| <i>temperature</i>      | FM    | temperature                                   |            | none      |                   |
| CONSTANT:               |       |   |            |           |                   |
| <i>PHYT<sub>0</sub></i> | FM    | inital biomass of phytoplankton               |            | none      |                   |
| <i>K<sub>c</sub></i>    | FM    | parameter of temperature function             |            | none      |                   |
| <i>K<sub>sr</sub></i>   | FM    | half saturation of solarradiation             |            | none      |                   |
| <i>K<sub>pd</sub></i>   | FM    | half saturation of phosphorous                |            | none      |                   |
| <i>K<sub>nt</sub></i>   | FM    | half saturation of nitrogen function          |            | none      |                   |
| <i>G<sub>phyt</sub></i> | FM    | value is adjusted for the maximum growth rate |            | none      |                   |
| TIME:                   |       |   |            |           |                   |
| <i>t</i>                |       | time  |            |           |                   |

\*) 1.character: alphanumeric(A) or float(F) or integer(I)

2.character: metric(M) or ordinal(O) or nominal(N)

## 7.2 Equation(s)

### 7.2.1 Initial state of the system ( $t \doteq 0$ ) :

$$\text{Bound: } PHYT = PHYT_0 \quad (7)$$

### 7.2.2 dynamics of phytoplankton Equationblock(1)

$$\frac{dPHYT}{dt} = GROWTH - LOSS - GRAZZ \quad (8)$$

$$LOSS = PHYT \cdot 0.5 \quad (9)$$

### 7.2.3 growth Equationblock(1)

$$GROWTH = G_{max} \cdot MM_{sr} \cdot MM_{pd} \cdot MM_{nt} \quad (10)$$

$$G_{max} = G_{phyt} \cdot e^{K_c \cdot temperature} \quad (11)$$

$$MM_{sr} = \frac{\text{solarradiation}}{K_{sr} + \text{solarradiation}} \quad (12)$$

$$MM_{pd} = \frac{\text{phosphorus}}{K_{pd} + \text{phosphorus}} \quad (13)$$

$$MM_{nt} = \frac{\text{nitrate}}{K_{nt} + \text{nitrate}} \quad (14)$$

### 7.3 Description of MATH module

Phytoplankton is a collection of several species of algae. For growing we consider input of the nutrients nitrate and phosphor , temperature and light(solar radiation). LOSS describes the loss by respiration and mortality of phytoplankton. GRAZZ is the predation of zooplankton on phytoplankton.

## 8 MATH: fish (Version: 1)

**Author:** Angelini,Ronaldo

**Documented by:** Noeding,Dirk

**Model (Origin of this mathematical formulation):**

ELLOBO; A model for the plankton system of the Broa reservoir, Sao Carlos, Brazil

**References:** [Ang00]

**Keywords:** predation, fish

**Simtype:** DYNAMIC

### 8.1 Declaration of Variables

| acronym              | type* | description   | time scale | time agg. | intime/state type |
|----------------------|-------|---|------------|-----------|-------------------|
| DEPENDENT:           |       |   |            |           |                   |
| <i>pred</i>          | FM    | zooplankton biomass and predation rate                |            | none      |                   |
| <i>loss</i>          | FM    | keep alive rate and mortality of fish                 |            | none      |                   |
| STATE:               |       |   |            |           |                   |
| <i>F</i>             | FM    | population of fishes                                  |            | none      | CONTINUOUS        |
| INPUT:               |       |   |            |           |                   |
| <i>Z</i>             | FM    | calculated zooplankton biomass                        |            | none      |                   |
| CONSTANT:            |       |   |            |           |                   |
| <i>K<sub>l</sub></i> | FM    | calculated fish mortality and keep alive rate per day |            | none      |                   |
| <i>K<sub>p</sub></i> | FM    | calculated zooplankton predation rate per day         |            | none      |                   |
| TIME:                |       |   |            |           |                   |
| <i>t</i>             |       | time  |            |           |                   |

\*) 1.character: alphanumeric(A) or float(F) or integer(I)

2.character: metric(M) or ordinal(O) or nominal(N)

### 8.2 Equation(s)

**8.2.1 Initial state of the system** ( $t \doteq 0$ ) :

**Bound:**  $F = 10$  (15)



### 8.2.2 fish Equationblock(1)

$$\frac{dF}{dt} = pred - loss \quad (16)$$

$$pred = Z \cdot K_p \quad (17)$$

$$loss = F \cdot K_l \quad (18)$$

## 9 Domain: ELLOBO

### 9.1 Classification of Domain

|  |   |
|--|---|
| <b>Soil classification (FAO):</b>              | any   |
| <b>Soil texture (US-Soil classification):</b>  | any   |
| <b>Climate classification (Walther/Lieth):</b> | <b>II</b> tropical and subtropical area<br><b>swr</b> dominant winter rain  |
| <b>Type of ecosystem (Ellenberg):</b>          | Oligotrophic_Lakes<br>Mesotrophic_Lakes   |
| <b>Biological classification:</b>              | Fish Astyanay fasciats<br>Phytoplankton serveral species<br>Zooplankton Argyrodiaptomus furcatus<br>Cladocera<br>Rotifers |

#### 9.1.1 Description of Domain

mean depth 3.0m

## References

- [Ang00] Ronaldo Angelini. A model for the plankton system of the broa reservoir sao carlos, brazil. *Ecological Modelling*, 126:131–137, 2000.
- [Joe83] S.E. Joergensen. *Application of Ecological Modelling in Environmental Management*, volume Part A. Elsevier Scientific Publishing Company, 1983.